

Forward-looking bidding in online auctions

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Let's buy a digital camera on eBay...



Canon S30, *15 mins left*

Canon S40, *33 mins left*

Olympus D40, *45 mins left*

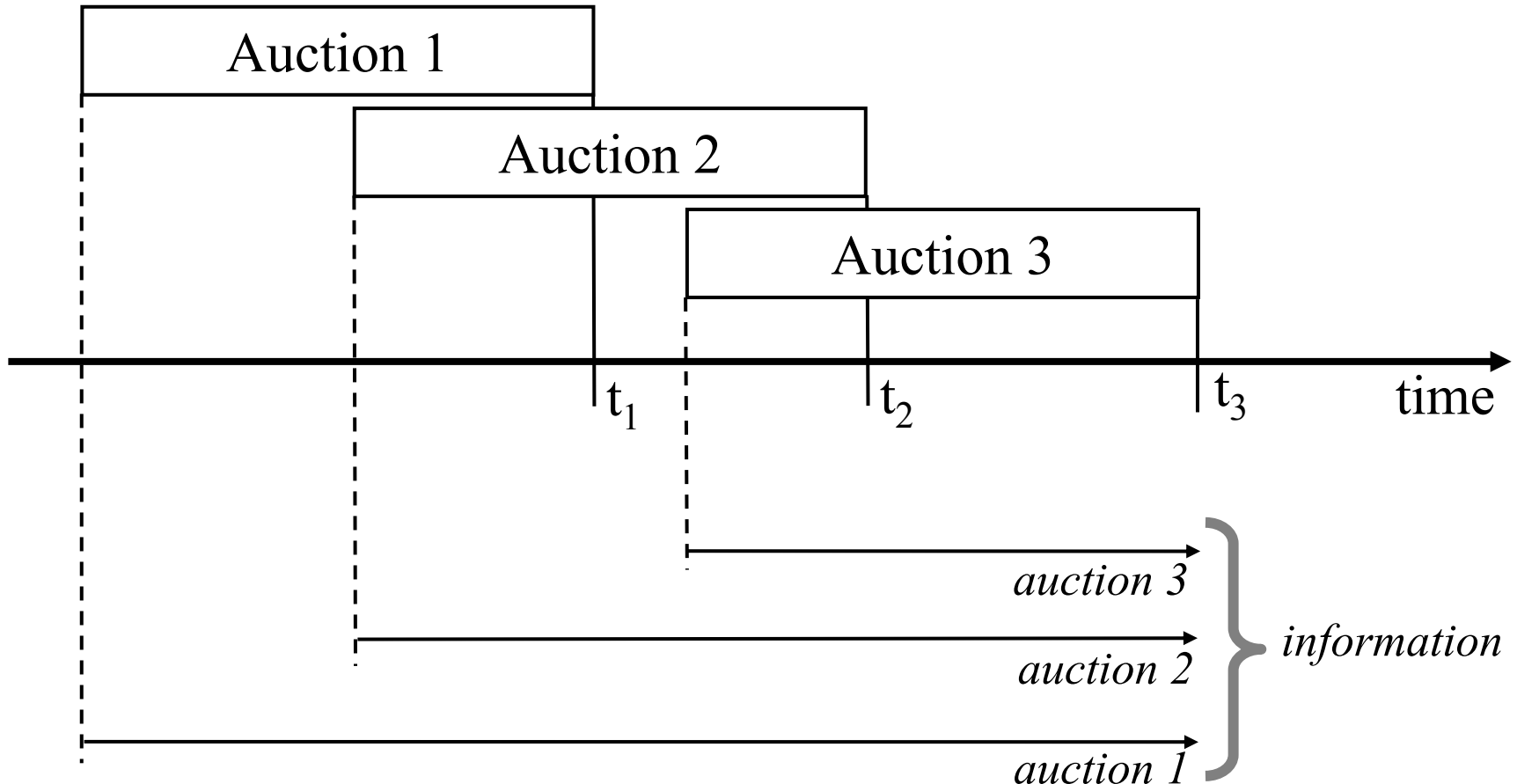
Canon S30, *47 mins left*

Olympus D40, *53 mins left*



- Electronics, movies, computers ... each buyer only wants one unit
- Population heterogeneity in preferences (I am shopping for Canon S30)
- Simultaneous? No, sequential, implicitly organized by end time
- Interlaced sequences of auctions for essentially identical objects

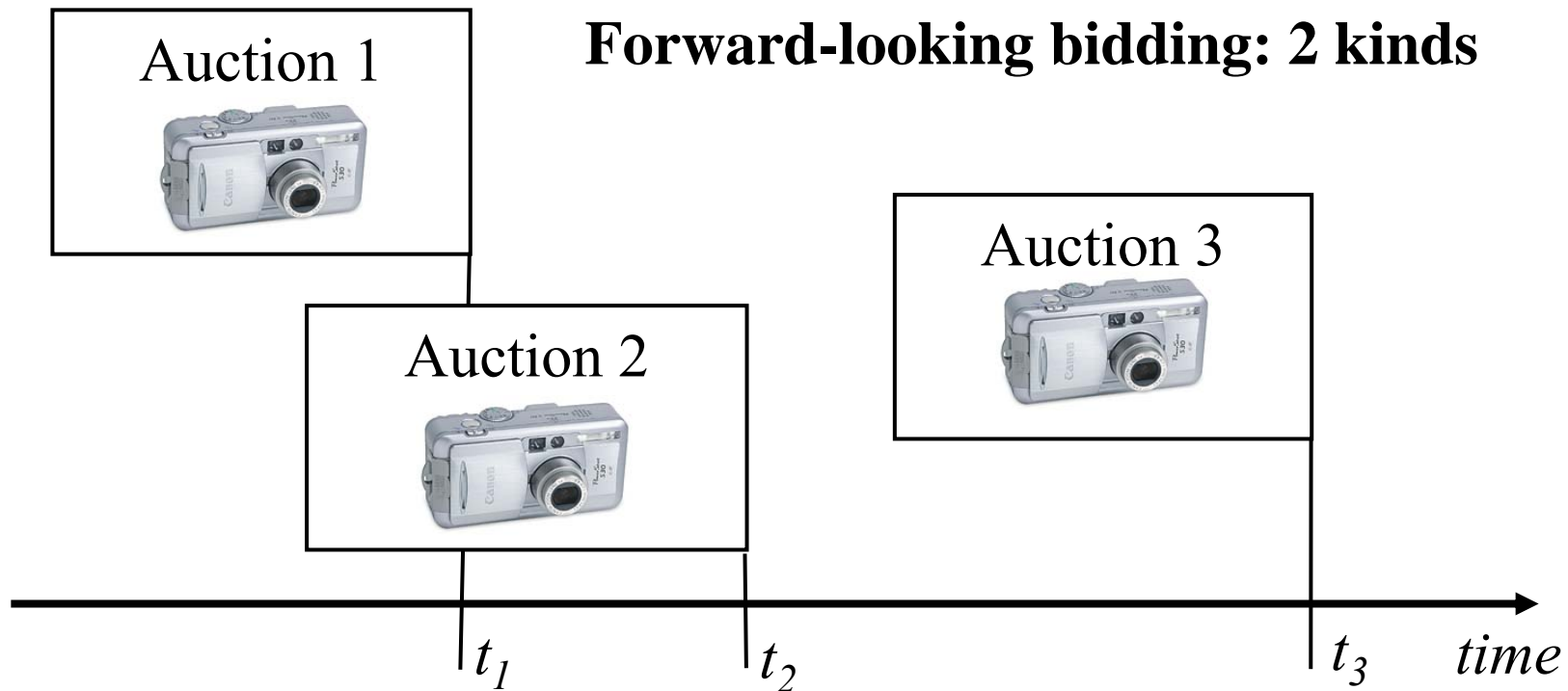
eBay: sequential auctions with overlapping information



Research questions:

- 1) How to bid while incorporating the available information?
- 2) Do eBay bidders bid consistently with the theory?

Forward-looking bidding: 2 kinds



unit-demand \rightarrow **option-value of losing** \rightarrow bid-shading (below isolated auction)

How to bid in auction 1?

- given the known (“forward-seen”) auction 2
- given a potential (“yet unseen”) auction 3 (Jofre-Bonet & Pesendorfer 03)

Some related work (all unit-demand bidders)

- **Milgrom & Weber (82b,99) :**
 - finite sequences , identical units
 - no use for information about future auctions (all the same)
 - finite \rightarrow no bidder-replacement needed \rightarrow elegant solution
- **Engelbrecht-Wiggans (94) , Jofre-Bonet & Pesendorfer (03) :**
 - finite sequences, stochastically equivalent units (different but *iid* units)
 - no information about future auctions \rightarrow symmetric and independent future
- **Gale & Hausch (94) :**
 - two auctions, different and potentially correlated units
 - $(v_1, v_2) \sim$ continuous F , both (v_1, v_2) known at the start
 - units not necessarily identical \rightarrow disposal issues
 - very hard to extend to many auctions
 - Contrast: I will only allow $v_i \in \{v, 0\} \approx \{"desired", "other"\}$

Model: One-period look-ahead, 2-type example

Infinite sequence of second-price, sealed-bid auctions

- varying waiting-times ω between individual auctions
- each auction sells one unit of a type- k good, $k: \{1,2\}$, $\Pr(k=1) = \frac{1}{2}$
- no reserve

N_k bidders present in every period, live until win or exit ($\Pr(exit)=\lambda$ per hour)

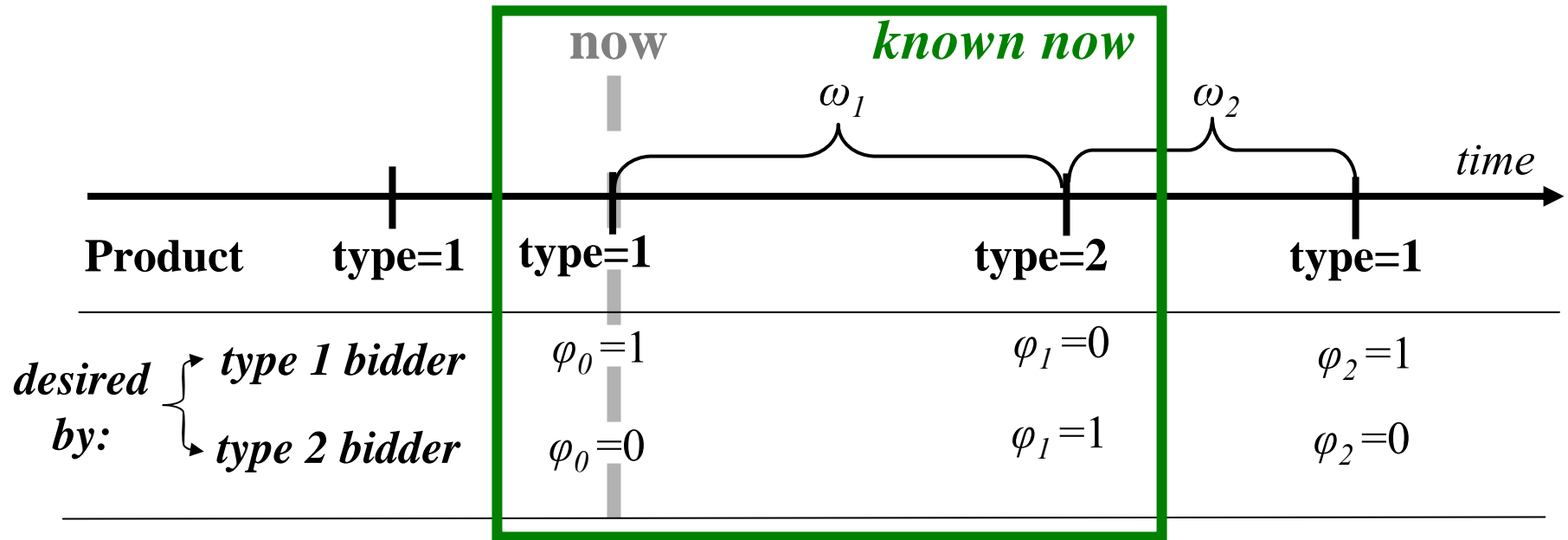
- unit-demand for only one type of good (“desired” type)
- IPV single-unit valuation of desired type, $v \sim F$ continuous
- **Info**: binary desirability of current unit φ_0 and next unit φ_1 , waiting-time ω_1

Everyone discounts future δ per hour, no memory

Discussion of the assumptions

- Interlaced sequences of identical-goods auctions with non-overlapping pop.
- Some bidder-replacement essential (otherwise steady-state survivors $v=0$)
- Innovation: bids depend on forward-seen information (ω_1, φ_1)

Model: One-period look-ahead, 2-type example



$S(\varphi_0, \varphi_1, \omega_1, v_i | c_0)$: expected surplus given loss to current competitive bid $c_0 \sim G$

$$b(\varphi_0, \varphi_1, \omega_1, v) = \arg \max_{\beta} \underbrace{\int_{\beta}^{\beta} (\varphi_0 v - c_0) dG(c_0)}_{\text{surplus if win now \& pay } c_0} + \underbrace{(\delta \lambda)^{\omega_1} \int_{\beta}^{\beta} S(\varphi_0, \varphi_1, \omega_1, v | c_0) dG(c_0)}_{\text{surplus if lose now to a bid } c_0}$$

Annotations for the equation:

- φ_0 : 1(current desired)
- φ_1 : 1(next desired)
- ω_1 : time till next
- v : valuation of desired

The two terms in the equation are connected by a double-headed arrow labeled **key tradeoff**.

Optimal Forward-Seeing Bidding

$$b(\varphi_0, \varphi_1, \omega_1, v) = \arg \max_{\beta \geq 0} \int_0^{\beta} (\varphi_0 v - c_0) dG(c_0) + (\delta \lambda)^{\omega_1} \int_{\beta} S(\varphi_0, \varphi_1, \omega_1, v | c_0) dG(c_0)$$

$$\text{FOC: } b(1, \varphi_1, \omega_1, v) = v - (\delta \lambda)^{\omega_1} S(1, \varphi_1, \omega_1, v | c_0 = b(1, \varphi_1, \omega_1, v)) < v$$

$$b(0, \varphi_1, \omega_1, v) = 0$$

$$\text{SOC: } \frac{\partial S(1, \varphi_1, \omega_1, v | c_0)}{\partial c_0} > -\frac{1}{(\lambda \delta)^{\omega_1}}$$

Properties:

- can show FOC has a unique solution, and that SOC satisfied
- bid-shading (a benefit to losing compared to isolated 2PSB)
- “pivotal thinking” : bid as if about to lose in a tie to a bidder like you

Equilibrium

Bellman condition: In a symmetric pure-strategy Markov-Perfect equilibrium, the expected surplus function must be “correct”:

$$S(\varphi_{0,1}, \omega_1, v | c_0) = E_{\varphi_2, \omega_2} \left[\int_{b(\varphi_{1,2}, \omega_2, v)}^{b(\varphi_{1,2}, \omega_2, v)} (v - c_1) dG(c_1 | c_0, \varphi_{0,1,2}, \omega_{1,2}) + (\delta \lambda)^{\omega_2} \int_{b(\varphi_{1,2}, \omega_2, v)} S(\varphi_{1,2}, \omega_2, v | c_1) dG(c_1 | c_0, \varphi_{0,1,2}, \omega_{1,2}) \right]$$

S exists when F has a continuous density on a compact interval.

For a given F , S can be obtained by value-function iteration.
Could this be a basis for a structural approach?

Bidders are not price-takers, take into account evolution of the pool of competitors.

Properties of equilibrium bidding

$$b(\varphi_0, \varphi_1, \omega_1, \nu)$$

Empirical strategy:

- positive only on desired type: $b = 0 \leftrightarrow \varphi_0 = 0$
 - increase in waiting time ω_1
 - decrease in desirability of the forward-seen type φ_1 (1 vs. 0)
 - increasing in ν on desired type
- } *assume
(identification)*
- } *test*
- } *look at order
stats given N*

Reduced-form test of model predictions

- 1) $K+1$ types, multi-period look-ahead with timing (**type-independent**) information Ω and product (**type-specific**) information Φ
 - eBay bidders usually see about a week ahead, could be many periods
 - Ω : auctions ending within the next hour marked in **red**, easy to see
- 2) Focus on a particular subset x of the state-variables (Ω, Φ) and integrate out the rest of the state, i.e. generate “on average” predictions given x :
$$\bar{b}(x, v) = E[b(1, \Phi, \Omega, v) | x] \quad (\text{example: } x = \# \text{ auctions ending within next hour})$$
- 3) If something is true for every valuation v , it will be true for the order-statistics of the valuations within each auction (keeping N constant)
- 4) Note that the first and second highest bids are observed in eBay data. \Rightarrow Regress bid order-statistics $b_{(j)}(x)$ on x (control for varying N)

Reduced-form test of forward-seeing bidding

Forward-seeing variables considered:

type-independent Ω :

- number of category auctions ending in the next hour

type-specific Φ :

- 1) time until next auction of the same type
- 2) 1(current type offered at least once within next five auctions)
- 3) {1(current type offered 1,2,3,4,5 auctions from now)}

} considered one
at a time

Regression specification:

$$\bar{b}_{(m),i} = \underbrace{\alpha_{m,type(i)}}_{\substack{\text{type/order} \\ \text{fixed-effect}}} + \underbrace{\beta_m \Omega_i}_{\substack{\text{type-indep.} \\ \text{forward-seeing}}} + \underbrace{\gamma_m \Phi_{i,type(i)}}_{\substack{\text{type-specific} \\ \text{forward-seeing}}} + \underbrace{\theta_m z_i}_{\text{controls:}} + \varepsilon_{m,i}$$

i : observation (listing) auction i sells type

m : order of the order-statistic (either 1 or 2)

- number of unique bidders
- seller reputation
- new vs. used dummy
- listing features (photo...)

Two different datasets from eBay

2 datasets

- 1 month of top 30 movies on DVD in 2002 (**type** = title), 3113 listings
- 4 months of MP3 players in 2001 (**type** = brand X model)
further split because prices vary a lot:
 - 15 Low-priced players (~\$70, +/- \$20), 1693 listings
 - 15 High-priced players (~\$180, +/- \$60), 2451 listings

Weaknesses of the data

- only seller-provided descriptions to identify types
- number of unique bidders not perfectly observed

→ 3 (datasets) x 2 (order-stats) x 3 (type-spec variables) = 18 regressions

Preliminary evidence for predicted behavior

- Most eventual winners won only one unit within the data-period (93% in MP3-players and 87% in movies).
- A substantial number of bidders participated in more than one auction (43% in MP3-players and 33% in movies) and those who did mostly stuck to bidding on one product-type.
- It does not seem that the multi-auction bidders simply submitted a very low bid initially to learn about the auction process or their true valuation, and only later raised their bid to their “full” willingness to pay. (Of the multi-bidders, 49% in movies and 59% in MP3 players submitted a higher second bid).

Regression results

Predicted effects : Number within category in next hour ↓, Time until next identical ↑,
Identical in next 5 auctions ↓, More distant future options gradually less effect.

DVD movies

type-independent: mostly not significant, predicted sign

type-specific : all as predicted:

- Average price ~\$10 → effect size on price: 3-7%

MP 3 players

type-independent: as predicted, but small (double number of auctions in next hour ~ 2 % ↓)

type-specific :

- Low-price players: not significant, predicted sign
- High-priced players : all as predicted
- Average price ~\$180 → effect size on price: 4-6% when the same type is available in the next 5 auctions, 1% when next delayed by 1 hour.

Regularity: 2nd highest bid (price) exhibits bigger effects than 1st highest bid. (?)

Discussion of the empirical findings

- Forward-seeing effects operate on eBay (3-7% price-reduction when the same type available within next 5 auctions, controlling for # bidders)
 - ⇒ Fairly high lower bound on bidder-sophistication
 - ⇒ Direction for specifying future more fine-grained structural models
 - ⇒ Analysts interested in demand-estimation should not interpret eBay auctions as repeated isolated auctions (downward bias)
- There may be forward-looking bid-shading beyond the reaction to already-listed “forward-seen” future auctions.
 - ⇒ Sellers may want to take note: such forward-looking bid-shading is a response to a seller strategy; bidding depends on selling and vice versa.
- Relevance beyond eBay: most sequences have look-ahead preannouncements...